Statistical Science Chapter 1.3 **Quantitative Reasoning**

Chapter 1.1 The Role of Statistics in Science Chapter 1.2 Model Based Statistics in Science
Lab 1 Verbal Models (Guess the Process)
Chapter 1.3 Quantitative Reasoning
Two Examples
Reasons for Model-Based Approach
on chalk board

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Not here last time?
Handout Syllabus
Questionnaire results
Yellow chalk
Lab 1
 Bring Cards
Location: cf syllabus
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Model Based Statistics in Science **ReCap.**

One Goal of this course is to introduce you to effective ways of thinking quantitatively about biological phenomena.

A second goal is to give you practice you need to increase your skill and confidence in the application of quantitative methods.

A third goal is to develop your critical capacity, both for your own work and that of others.

It is NOT a course in mathematics. It is a course in applied mathematics.

Limited treatment of mathematical apparatus.

Emphasis will be on applying this apparatus.

Will work with data, summarizations of data (tables, graphs, statistics, models). The emphasis will be on the practical application of quantitative methods to interesting questions and perplexing problems in science.

It IS a course in how to think with biologically interesting quantities.

Today Examples of Quantitative Reasoning

Wrap-Up

In this course we will adopt a model based approach to statistics. There are several advantages.

- Statistics and modelling are <u>closely related</u> stats are based on models. 1
- Advantage of integration is carryover 2
- We have a broader <u>capacity</u> to evaluate uncertainty in the analysis of biological data, 3 than if we learn a series of tests.
- Model approach leads to learning of concepts & principles, rather than collection of 4 techniques.

An example of quantitative reasoning

Statistics are traditionally taught separately from 'models'

Example of statistics: regression

Example of model: $N = N_o e^{rt}$ N = bacterial numbers, t = time.

This is an equation for exponential growth in bacterial numbers N

This course will integrate both equations and statistics in reasoning about biological problems. Here is an example.



We use a statistical technique (regression) to estimate r, the slope of the line.

The regression estimate is r = 0.006/hr or 0.6%/hour.

We rewrite the equation, this time with the estimated value of r. $N = N_o e^{0.6t}$ This is a <u>formal model</u> with a specific value of r.

A formal model states an idea about the relation of measured quantities (N and t), expressed in symbolic form. Here is a diagram of what we just did.



Construct triangle
Write DATA
Write VERBAL MODEL above DATA
connect to DATA with line
Write GRAPHICAL MODEL
connect to VERBAL MODEL by line
Write FORMAL MODEL
connect to GRAPHICAL with a line
to complete triangle

Another example of quantitative reasoning

 $M = K_2$ if R not equal 5 or 6

M = catch of scallops (kg)State verbal model. R = seabed roughness (acoustic values) Catch is higher in gravel than 28 measurements in finer (sand) or coarser (cobble) substrates 200 Ask for graphical model. 150 100 Draw this model in yellow. 50 Then draw other models М 0 - housetop, - two means, gravel or not 2 3 4 5 10 1 6 8 9 R - normal curve (gravel) (cobble) (sand) Write equation for two-mean model $M = K_1$ if R = 5 or 6 (gravel)

Draw data in white chalk.

Let's review what we did. We began with verbal model, then moved to graphical model, and finally to a formal model. This illustrates quantitative reasoning.

Both models can be	Data	=	Model	+	residual
compared to data.	М	=	K_1 if $R = 5$ or 6		reciduale
	Μ	=	K_2 if R not equal 5 or 6	т	residuais

The two-mean model happens to be the statistical model used in a t-test, which is a test of whether two means differ by more than just chance levels.

This format (Data = Model + Residual) integrates "modeling" with "statistics"

We are going to use models of data to summarize data, as in <u>descriptive statistics</u>. Common examples are means, standard deviations, and correlations.

We are going to use models to quantify uncertainty and draw conclusions from the data. This is called <u>inferential statistics</u>. It takes several forms.

- 1. Evidentialist. We infer from the data to a model of the data. We report likelihood ratios as a measure of the strength evidence calculated from our data.
- 2. Frequentist. We use likelihood ratios to infer from the data to a population.
- 3. Priorist. We use a likelihood ratio to infer from a prior to a posterior probability.

What then is a likelihood ratio? It is a measure of evidence for one model (say a regression line) relative to another (regression line with zero slope). In this course you will learn about and use both a measure of evidence (the likelihood ratio) and a measure of uncertainty (the p-value).

Reasons for model based approach to statistics.

Statistics are traditionally taught separately from 'models.'

Example of statistics: regression. Example of model: 1/N dN/dt = r

This course does not present statistics as a collection of tests. The course teaches you to write the statistical model based on a science question. Why this approach?

- REASON 1 With the modelling approach we are no longer dependant on the machinery of hypothesis testing. We have a <u>broader range</u> of ways to evaluate uncertainty in the analysis of biological data.
- REASON 2 Model approach leads to learning of <u>concepts & principles</u>, rather than memorizing a collection of techniques.
- REASON 3 Statistics and modelling are <u>closely related</u>. To illustrate: Models underlie the most widely used statistical methods. Statistical analysis is commonly used to develop and defend a model.
- REASON 4 A model-based approach has the advantage of <u>carryover</u>. We use what we know about biological models to improve statistical analysis We use what we know about statistics to evaluate models.

Statistics are traditionally taught as a series of techniques "101 Statistical Tests" This is the way we identify birds from a field guide. Or how we identify plants from a key. But it is not a description of how we do science.

Instead, we learn concepts that connect terms.

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To illustrate, scatter these 8 terms on board
sporophyte, metaphase, blastula, morula,
gametophyte, prophase, telophase, gastrula
Probably no one can still define these (I can't either)
But I bet you can still match them by concept
cell cycle
alternation of generations
early development (embryogenesis)
Which terms pertain to the concept of "Cell cycle" ?
(they'll get it right. draw circle around these terms.)
Which terms pertain to "Alternation of generations" ?
(students call out terms, draw circle around these)
Which terms pertain to "embryogenesis" ? etc.
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Reasons for modeling approach.

REASON 2. Learning concepts and principles. More about this.

Learning to write the model has several advantages

Work from general principles of survey and experimental design.

Reduction in arbitrary material to learn.

Extends analysis beyond the list of named tests.

Extends analysis beyond text-book cases, which don't always fit our data.

But there are <u>disadvantages</u>

Principles are abstract, and so are harder to learn.

We need specific cases, often several, to grasp a concept.

Statistics are often taught as series of prescriptions, because this is less abstract and all we have to do is follow the recipe.

A few prescriptions are highly useful, serving well in many cases (for example, t-test)

But while prescriptions are readily learned in a classroom setting (follow the recipe), they are not going to serve us well outside the classroom.

There may not be a textbook case that fits our data.

The search for a better recipe can be laborious and confusing.

We end up having to learn corrections (e.g. arcsin transform for % data).

The corrections may be a waste of time (*e.g.* arcsin transform).

Several prescriptions fit our data, but give different results

(e.g., ANOVA versus Kruskal Wallis test).

Standard prescriptions are more limited than writing the model

(*e.g.* Chisquare tests vs logistic regression model).

Some widely held beliefs are wrong (*e.g.* 'data must be normal').

Key assumptions are sometimes missing from the prescription

(*e.g.* homogeneity of slopes when using ANCOVA for statistical control). When we focus on learning a series of tests we don't learn general principles.

Principles and general techniques (*e.g.* constructing the model, evaluating the residuals) will serve us best when it comes to

designing an experiment, designing a survey,

evaluating statistical conclusions in the published literature.

Model based statistics – Course goals and course structure

Learning principles and how to implement them on a computer will serve us better than learning prescriptions. Learning prescriptions will not serve us well, beyond the classroom.

Methods and principles will be taught together in same course

-methods in the lab sections (including use of computer),

-principles in lectures.

The goal is to learn to think with quantities, as well as to develop skill in applying specific methods.

The course begins with the basics of data collection and explanatory models (Part I): the concept of a well defined, measurable Quantity working with models in symbolic form (practice in Lab 2) Part II covers quantitative measures of evidence and uncertainty: Frequency distributions Likelihood ratios Type I and II error Bayes' rule and confidence intervals Part III covers statistical analysis for a single explanatory variable. Linear regression t-tests One-way ANOVA Part IV covers statistical analysis for multiple explanatory variables. Multiple regression Multiway ANOVA

ANCOVA

Designs that do not fit into these categories.